# GIRLS' HIGH SCHOOL \& COLLEGE, PRAYAGRAJ 

SESSION:2020-21
CLASS: IX (A,B,C,D,E)
SUBJECT: MATHEMATICS
ASSIGNMENT-01

INSTRUCTIONS:The Parents to ensure that their ward watches the video instructions for this assignment by clicking on the given link:

## https://youtu.be/SeyF9bwdX74

She should revise the lesson given in the book and then work on the assignment. The completed assignment is to be downloaded and filed/ pasted in the subject file / copy and kept ready for submission. The day, date and procedure of submission shall be notified later.

> Reference Book:- Concise Mathematics Class IX - By R.K. Bansal

TOPIC: PYTHAGORAS THEOREM

Solve the following questions:

Q1.A ladder 13 m long rests against a vertical wall. If the foot of the ladder is 5 m from the foot of the wall, find the distance of the other end of the ladder from the ground.

Q2. A man goes 40 m due north and then 50 m due west. Find his distance from the starting point.

Q3. In a triangle $A B C$, given below, $A B=8 \mathrm{~cm}, B C=6 \mathrm{~cm}$ and $A C=3 \mathrm{~cm}$. Calculate the length of OC.


Q4 .Two poles of heights 6 m and 11 m stand vertically on a plane ground. If the distance between their feet is 12 m ; find the distance between their tips.

Q5.In a triangle $A B C$, angle $B=90^{\circ}$ Find the sides of the triangle, if:
(i) $A B=(x-3) c m, B C=(x+4) \mathrm{cm}$ and $A C=(x+6) \mathrm{cm}$.
(ii) $A B=x \mathrm{~cm}, B C=(4 x+4) \mathrm{cm}$ and $A C=(4 x+5) \mathrm{cm}$

Q6. In the figure given below, $A D$ is perpendicular to $B C$.
Prove that: $\quad c^{2}=a^{2}+b^{2}-2 a x$.

$Q 7 . A B C$ is a triangle, right-angled at $B . M$ is a point on $B C$. Prove that:

$$
A M^{2}+B C^{2}=A C^{2}+B M^{2}
$$

Q8. In a rectangle $A B C D$, prove that:

$$
A C^{2}+B D^{2}=A B^{2}+B C^{2}+C D^{2}+D A^{2}
$$

Q9. Diagonals of a rhombus $A B C D$ intersect each other at point $O$. Prove that:

$$
O A^{2}+O C^{2}=2 A D^{2}-\frac{B D^{2}}{2}
$$

Q10.In an isosceles triangle $A B C ; A B=A C$ and $D$ is a point on $B C$ produced. Prove that:

$$
A D^{2}=A C^{2}+B D \cdot C D
$$

Q11. In a triangle $A B C, A B=A C$ and $B D$ is perpendicular to $A C$. Prove that:

$$
\mathrm{BD}^{2}-\mathrm{CD}^{2}=2 \mathrm{CD} \times \mathrm{AD}
$$

Q12. $O$ is any point inside a rectangle $A B C D$. Prove that :

$$
O B^{2}+O D^{2}=O C^{2}+O A^{2}
$$

Q13.In a quadrilateral $A B C D$, angle $B=90^{\circ}$ and angle $D=90^{\circ}$. Prove that:

$$
2 A C^{2}-A B^{2}=B C^{2}+C D^{2}+D A^{2}
$$

Q14. In a triangle $A B C$, angle $B=90^{\circ}$ and $D$ is the midpoint of $B C$. Prove that:

$$
A C^{2}=A D^{2}+3 C D^{2}
$$

Q15. $M$ and $N$ are the midpoints of the sides $Q R$ and $P Q$ respectively of a triangle PQR, right-angled at Q. Prove that:
(i) $\mathrm{PM}^{2}+\mathrm{RN}^{2}=5 \mathrm{MN}^{2}$
(ii) $4 \mathrm{PM}^{2}=4 P Q^{2}+Q R^{2}$
(iii) $4 R N^{2}=P Q^{2}+4 Q R^{2}$
(iv) $4\left(P M^{2}+R N^{2}\right)=5 P^{2}$

Q16. In the figure : angle $\mathrm{PSQ}=90^{\circ}, \mathrm{PQ}=10 \mathrm{~cm}, \mathrm{QS}=6 \mathrm{~cm}$ and $\mathrm{RQ}=9$ cm . Calculate the length of PR.


Q17. If the sides of a triangle are in the ratio $1: \sqrt{2}: 1$, show that it is a right-angled triangle.

Q18. In equilateral triangle $A B C, A D$ is perpendicular to $B C$ and $B C=x$ cm . Find, in terms of $x$, the length of $A D$.

Q19. In the following figure, $A D$ is perpendicular to $B C$ and $D$ divides $B C$ in the ratio 1:3. Prove that:

$$
2 A C^{2}=2 A B^{2}+B C^{2}
$$



Q20. In a triangle $A B C, A B=A C=x ; B C=10 \mathrm{~cm}$ and the area of the triangle is $60 \mathrm{~cm}^{2}$. Find x .

## END

